# Registers and Counters Assigned Date: Eleventh Week Due Date: Apr. 7, 2014 

P1. (10 points) Consider the master-slave D flip-flop design in Figure 5.9(a) in textbook. For the input Clock and $D$ given below, please draw a timing diagram for $Q_{m}$ and $Q_{s}$. Then briefly explain why this flip-flip design is negative-edge triggered.


P2. (10 points) Problem 5.7 in textbook.

P3. (10 points) This question considers the construction of a 32-bit register with transistors. Suppose D flip-flops are implemented as shown in Figure 5.9(a) in which gated D latches are implemented as shown in Figure 5.7(a) in textbook. The NAND gates and NOT gates used are implemented as CMOS circuits as discussed in Appendix B. How many transistors are required to implement a 32-bit register?

P4. (20 points) Design a 4-bit register with both shift and parallel load features. The inputs of the register include a 2-bit control code $\mathrm{X} Y$, a 4-bit input value I 3 I 2 II IO , and a clock signal. The outputs of the register are the 4 bits Q3 Q2 Q1 Q0 corresponding to the value stored in the register. You are allowed to use any number of $D$ flip-flops, muxes of any size, decoders and encoders of any sizes, AND gates, OR gates, and NOT gates. (Notice that you do not need all of them.) The operations of the register is defined below:

## XY Operation

00 Hold the current value stored (i.e., Q3 Q2 Q1 Q0 are not changed)
01 Shift right (i.e., new Q3=13, new Q2=Q3, new Q1=Q2, new $Q 0=Q 1$ )
10 Shift left (i.e., new Q3=Q2, new Q2=Q1, new Q1=Q0, new $Q 0=10$ )
11 Load new date (i.e., new $Q 3=13$, new $Q 2=12$, new $Q 1=11$, new $Q 0=10$ )
P5. (10 points) To construct a register file containing 168 -bit registers, one input port and three output ports, we use w 8-bit registers with parallel load input, $\mathbf{x} \mathbf{y}$-to-1 $\mathbf{z}$-bit muxes, and $\mathbf{p} \mathbf{q}$-to-r decoder with enable. Specify the values of $\mathbf{w}, \mathbf{x}, \mathbf{y}, \mathbf{z}, \mathbf{p}, \mathbf{q}$, and $\mathbf{r}$.

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P6. (15 points) Design a 4-bit asynchronous up/down-counter with Enable using T flip-flops and any combinational circuit devices. The direction of the counter is controlled by a 1-bit signal U . If $\mathrm{U}=1$, the counter will count up. If $\mathrm{U}=0$, the counter will count down. The counting can be enabled/disabled by a 1-bit signal E . If $\mathrm{E}=1$, the counter will count whenever there is up-going clock edge. If $\mathrm{E}=0$, the counter will keep the same value stored.

P7. (15 points) Design a 4-bit asynchronous up-counter using JK flip-flops. (Hint: Think of how to implement a T flip-flop using a JK flip-flop.)

P8. (10 points) Bob needs to use a 3-bit down-counter. However, he only has a 4-bit synchronous up-counter and several NOT gates. He is NOT allowed to modify the internal structure of the up-counter. How can he construct the 3-bit down-counter using only the devices he has?

