

- P1. (10 points) Problem 6.23 in your textbook.
- P2. (10 points) Problem 6.24 in your textbook.
- P3. (10 points) Problem 6.25 in your textbook.
- P4. (10 points) Consider the state machine specified by the following state transition table.

Current	Input	Next
X Y	I	X Y
0 0	0	1 1
0 0	1	0 1
0 1	0	0 0
0 1	1	1 0
1 0	0	0 1
1 0	1	1 1
1 1	0	1 0
1 1	1	0 0

- (a) Draw the state transition diagram of the machine.
- (b) Write two next-state expressions for X and Y that will implement the transitions of the state machine. Please make your expressions as simple as possible, and use XOR gates and NOT gates only.
- (c) Implement the state machine using D flip-flops, XOR gates, and NOT gates.
- (d) Suppose the machine is initially in 00 (i.e., X=0 and Y=0). Indicate for each input sequence below, the state the machine is in after the last digit has been read in. Assume the digits are read in from left to right.
- 111111
  - 10011000011100
  - 432 1s followed by 321 0s

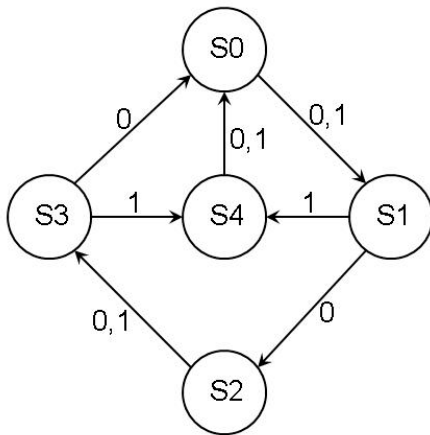
P5. (10 points) Design a state machine with three output bits. The machine will repeatedly output the sequence 100, 101, 111, 111, 000, 001, 011, 011.

- (a) Draw a state diagram for the machine.
- (b) Write a truth table for the next state logic and the output logic.
- (c) Simplify the expressions for the next state logic and the output logic using K-maps.
- (d) Implement the state machine using D flip-flops, AND gates, OR gates, and NOT gates.

P6. (10 points) A state machine has no input (except a clock input) and a single bit output Q. The value of Q is 1 if and only if the number of clock ticks (after reset) is either a multiple of 2 or a multiple of 3. Otherwise, the value of Q is 0. Draw a state diagram for the state machine using as few states as possible (Hint: More than three states are required).

P7. (10 points) A state machine has one input P in addition to the clock input and one output Q. The value of Q is 1 if and only if the number of 1's in the sequence of input P is not divisible by 2 and not divisible by 3. Otherwise, the output value Q is 0. Draw a state transition diagram for the state machine using as few states as possible.

P8. (10 points) Give a state-assigned next state table corresponding to the state diagram given below. Note that you have one input variable, W. A transition labeling of "0, 1" means that the input can be either 0 or 1. Write the state assignment clearly. Label your table appropriately.



P9. (10 points) (a) Draw a state transition diagram for a state machine that reads in a sequence of binary digits, one at a time, and stops when it has read in five 1s (need not be consecutive). To "stop" the machine, merely have it loop in the state it reaches after a successful match. (b) Now draw a state transition diagram for a state machine that stops when it has read in at least three consecutive 1s followed by a 0.

P10. (10 points) Design a three-bit counter-like circuit controlled by the input w. If w=0, then the counter subtracts 1 from its contents (acting like a normal down-counter). If w=1, then the counter adds 2 to its contents, wrapping around if the count has to become 8 or 9. Thus if the current state is 6 (or 7) and w=1, then the next state is 0 (or 1). Use D flip-flops in your circuit.