

## CprE 281: Digital Logic

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#### http://www.ece.iastate.edu/~alexs/classes/

## **Floating Point Numbers**

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## **Administrative Stuff**

- HW 6 is out
- It is due on Monday Oct 12 @ 4pm

## The story with floats is more complicated IEEE 754-1985 Standard



[http://en.wikipedia.org/wiki/IEEE\_754]



s = +1 (positive numbers and +0) when the sign bit is 0

s = -1 (negative numbers and -0) when the sign bit is 1

e = exponent - 127 (in other words the exponent is stored with 127 added to it, also called "biased with 127")

In the example shown above, the *sign* is zero so s is +1, the *exponent* is 124 so e is -3, and the significand m is 1.01 (in binary, which is 1.25 in decimal). The represented number is therefore +1.25 × 2<sup>-3</sup>, which is +0.15625.

[http://en.wikipedia.org/wiki/IEEE\_754]



Figure 3.37. IEEE Standard floating-point formats.

## **On-line IEEE 754 Converter**

<u>http://www.h-schmidt.net/FloatApplet/IEEE754.html</u>

#### Conversion of fixed point numbers from decimal to binary

Convert (214.45)10



[Figure 3.44 from the textbook]

## Memory Analogy



Address 0

**Address 1** 

Address 2

Address 3

Address 4

Address 5

Address 6

## Memory Analogy (32 bit architecture)



Address4Address8Address12Address16

Address 0

- Address 20
- Address 24

## Memory Analogy (32 bit architecture)



Address 0x00 Address 0x04 Address 0x08 Address 0x0C Address 0x10 Address 0x14 Address 0x18 Hexadecimal

## **Storing a Double**

Address 0x08

Address 0x0C



## Storing 3.14

- 3.14 in binary IEEE-754 double precision (64 bits)
- In hexadecimal this is (hint: groups of four):

0100 0000 0000 1001 0001 1110 1011 1000 0101 0001 1110 1011 1000 0101 0001 1111 4 0 0 9 1 E B 8 5 1 E B 8 5 1 F

## Storing 3.14

- So 3.14 in hexadecimal IEEE-754 is 40091EB851EB851F
- This is 64 bits.
- On a 32 bit architecture there are 2 ways to store this



## Storing 3.14

Address 0x08

Address 0x0C



**Big-Endian** 

Little-Endian

Address 0x08

Address 0x0C



### Storing 3.14 on a Little-Endian Machine (these are the actual bits that are stored)



#### Once again, 3.14 in IEEE-754 double precision is:

exponent

mantissa

sign

0

## They are stored in binary the hexadecimals are just for visualization





http://en.wikipedia.org/wiki/Endianness

## **Little Endian**



http://en.wikipedia.org/wiki/Endianness

## **Big-Endian/Little-Endian analogy**



[image fom http://www.simplylockers.co.uk/images/PLowLocker.gif]

## **Big-Endian/Little-Endian analogy**



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## **Big-Endian/Little-Endian analogy**



[image fom http://www.simplylockers.co.uk/images/PLowLocker.gif]

# What would be printed? (don't try this at home)

```
double pi = 3.14;
printf("%d",pi);
```

• Result: 1374389535

- 3.14 = 40091EB851EB851F (in double format)
- Stored on a little-endian 32-bit architecture
  - 51EB851F (1374389535 in decimal)
  - 40091EB8 (1074339512 in decimal)

# What would be printed? (don't try this at home)

```
double pi = 3.14;
printf("%d %d", pi);
```

• Result: 1374389535 1074339512

- 3.14 = 40091EB851EB851F (in double format)
- Stored on a little-endian 32-bit architecture
  - 51EB851F (1374389535 in decimal)
  - 40091EB8 (1074339512 in decimal)
  - The second %d uses the extra bytes of pi that were not printed by the first %d

# What would be printed? (don't try this at home)

double a = 2.0;
printf("%d",a);

• Result: 0

- 2.0 = 40000000 00000000 (in hex IEEE double format)
- Stored on a little-endian 32-bit architecture
  - 00000000 (0 in decimal)
  - 40000000 (1073741824 in decimal)

## What would be printed? (an even more advanced example)

• Result: 1374389535 1074339512

- 3.14 = 40091EB851EB851F (in double format)
- Stored on a little-endian 32-bit architecture
  - 51EB851F (1374389535 in decimal)
  - 40091EB8 (1074339512 in decimal)
- The double 3.14 requires 64 bits which are stored in the two consecutive 32-bit integers named a[0] and a[1]

## **Questions?**

### THE END