

P1. (10 points) Prove that the following are true (using truth tables):

- a) $A \oplus B = \overline{A \oplus B}$
- b) $\overline{A \oplus B} = A \oplus B$

P2. (10 points) Show how to implement a NOT function by using:

- a) a 2-input NAND gate only. (5 points)
- b) a 2-input NOR gate only. (5 points)

For part (a) and part (b), you should use **a different way from what has been shown in class** (connecting both terminals to the input signal). Note that you are allowed to connect constant voltages (i.e., logic values 0 or 1) to the gate inputs.

P3. (10 points) Implement the following functions using only NAND gates:

- a) $F = AB + \overline{BC}$
- b) $F = A\overline{B} + (\overline{B} + \overline{C})\overline{A}$

P4. (10 points) Implement the following functions using only NOR gates:

- a) $F = (A + B)(\overline{A} + \overline{B})$
- b) $F = A(B + C)(\overline{D} + E)$

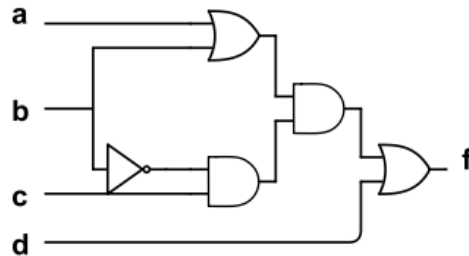
P5. (20 points) A logic circuit has three inputs P , Q , R and one output S . The value of S is equal to 1 whenever $P = 0$ or whenever $Q = R = 1$.

- a) Derive the truth table for this circuit. (5 points)
- b) Use Boolean algebra to derive the simplified expression from the canonical SOP form. (5 points)
- c) Draw the logic circuit for the simplified Boolean expression using only AND, OR, and NOT gates. (5 points)
- d) Draw the logic circuit for the simplified Boolean expression using only NAND gates. (5 points)

P6. (20 points) Design a majority voting machine with three inputs A , B , C and one output F . $F = 1$ when at least two of the inputs are equal to 1 (e.g., $A = 1$, $B = 1$, $C = 0$), and $F = 0$ when the majority of the inputs are equal to 0 (e.g., $A = 0$, $B = 1$, $C = 0$).

- a) Derive the truth table for the voting machine. (5 points)
- b) Use Boolean algebra to derive the simplified expression from the canonical SOP form. (5 points)
- c) Draw the logic circuit for the simplified Boolean expression using only AND, OR, and NOT gates. (5 points)
- d) Draw the logic circuit for the simplified Boolean expression using only NAND gates. (5 points)

P7. (10 points) Write down the Verilog code for the following circuit by using gate-level primitives.



P8. (10 points) Write down the Verilog code for the circuit from P7, but this time use continuous assignments.