# Synchronous Sequential Circuits <br> Assigned Date: Twelfth Week <br> Due Date: Monday, Nov. 14, 2016 

P1. (10 points)
Briefly explain the major difference between a Moore state machine and a Mealy state machine.
P2. (25 points)
A FSM with an input $w$ and an output $z$ has the following state table.

| Present <br> State | Next State |  | Output $z$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $w=0$ | $w=1$ | $w=0$ | $w=1$ |
| A | A | B | 0 | 1 |
| B | C | B | 1 | 0 |
| C | B | A | 0 | 0 |

a) (5 points) Draw the state diagram based on the state table.
b) (5 points) Complete the state-assigned table based on the state table.

| Present <br> State | Next State |  | Output $z$ |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | $y_{1}=0$ | $w=1$ | $w=0$ | $w=1$ |  |
| A | $y_{1} y_{0}$ | $Y_{1} Y_{0}$ | $Y_{1} Y_{0}$ | $z$ | $z$ |
|  | 0 |  |  |  |  |
| C | 0 | 1 |  |  |  |
| 1 | 1 |  |  |  |  |
|  |  |  |  |  |  |

c) (5 points) Find the simplified SOP expressions for $Y_{1}, Y_{0}$, and $z$.
d) (5 points) Draw the circuit diagram using D flip-flops and any other required gates.
e) (5 points) Is this a Moore machine or a Mealy machine? Why?

P3. (15 points)
A FSM has two D flip-flops, an input $w$, and an output $z$. The circuit diagram is shown below.

a) (5 points) Find the logic expressions of $Y_{1}, Y_{0}$, and the output $z$.
b) ( 5 points) Show the state-assigned table of the FSM.
c) ( 5 points) Draw the state diagram of the FSM.

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## P4. (10 points)

A two-bit counter has the following circuit diagram. The output is $z_{1} z_{0}=y_{1} y_{0}$.

a) (5 points) Draw the state diagram of the counter.
b) (5 points) What is the repeated counting sequence of this counter?

P5. ( 30 points)
Consider the following state table for a FSM.

| Present <br> State | Next State |  | Output |
| :---: | :---: | :---: | :---: |
|  | $w=0$ | $w=1$ | $z$ |
| A | A | B | 0 |
| B | B | C | 1 |
| C | C | D | 0 |
| D | D | A | 1 |

a) (5 points) Draw the state diagram of the FSM.
b) (5 points) Draw the circuit diagram of FSM using D flip-flops.
c) (5 points) Perform state minimization to minimize the number of states. Show your partitions in the procedure.
d) (5 points) Draw the new state diagram of the minimized FSM.
e) (5 points) Draw the circuit diagram of the minimized FSM using D flip-flops.
f) (5 points) Compare the circuits in (b) and (e), what is the benefit of state minimization?

## P6. (10 points)

Bob needs to use a 3-bit up-counter. However, he only has a 4-bit synchronous down-counter and several NOT gates. He is NOT allowed to modify the internal structure of the down-counter. How can he construct the 3-bit up-counter using only the devices that he has?

