

## CprE 281: Digital Logic

## Instructor: Alexander Stoytchev

http://www.ece.iastate.edu/~alexs/classes/

# NAND and NOR Logic Networks 

CprE 281: Digital Logic
Iowa State University, Ames, IA
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## Administrative Stuff

- HW2 is due on Wednesday Sep 7


## Administrative Stuff

- HW3 is out
- It is due on Monday Sep 12 @ 4pm.
- Please write clearly on the first page (in BLOCK CAPITAL letters) the following three things:
- Your First and Last Name
- Your Student ID Number
- Your Lab Section Letter
- Staple all of your pages together
- If any of these are missing, then you will lose $10 \%$ of your grade for that homework.


## Labs Next Week

- If your lab is on Mondays, $\mathbf{i , e} .$,
- Section N: Mondays, 9:00-11:50 am (Coover Hall, room 1318)
- Section P: Mondays, 12:10-3:00 pm (Coover Hall, room 1318)
- Section R: Mondays, 5:10-8:00 pm (Coover Hall, room 1318)
- You will have 2 labs in one on September 12.
- That is, Lab \#2 and Lab \#3.


## Labs Next Week

- If your recitation is on Mondays, please go to one of the other 9 recitations next week:
- Section U: Tuesday 11:00 AM - 1:50 PM (Coover Hall, room 2050) Section M: Tuesday 2:10 PM - 5:00 PM (Coover Hall, room 2050) Section J: Wednesday 8:00 AM - 10:50 AM (Coover Hall, room 2050) Section T: Wednesday 6:10 PM - 9:00 PM (Coover Hall, room 1318) Section Q: Thursday 11:00 AM - 1:50 PM (Coover Hall, room 2050) Section V: Thursday 11:00 AM - 1:50 PM (Coover Hall, room 1318) Section L: Thursday 2:10 PM - 5:00 PM (Coover Hall, room 2050) Section K: Thursday 5:10 PM - 8:00 PM (Coover Hall, room 2050) Section G: Friday 11:00 AM - 1:50 PM (Coover Hall, room 2050)
- This is only for next week. And only for the recitation (first hour). You won't be able to stay for the lab as the sections are full.


## Quick Review

## The Three Basic Logic Gates



NOT gate


AND gate


OR gate

## Truth Table for NOT



## Truth Table for AND



| $x_{1}$ | $x_{2}$ | $x_{1} \cdot x_{2}$ |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

## Truth Table for OR



| $x_{1}$ | $x_{2}$ | $x_{1}+x_{2}$ |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 1 |

## DeMorgan's Theorem

## 15a. <br> $\overline{\mathrm{x} \cdot \mathrm{y}}=\overline{\mathrm{x}}+\overline{\mathrm{y}}$ <br> 15b. <br> $\overline{\mathbf{x}+\mathbf{y}}=\overline{\mathbf{x}} \cdot \overline{\mathbf{y}}$

## Synthesize the Following Function

| $\mathbf{x}_{1}$ | $\mathbf{x}_{2}$ | $\mathbf{f}\left(\mathbf{x}_{1}, \mathbf{x}_{2}\right)$ |
| :---: | :---: | :---: |
| 0 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

## Split the function into 4 functions

| $\mathbf{x}_{1}$ | $\mathbf{x}_{2}$ | $\mathrm{f}_{00}\left(\mathbf{x}_{1}, \mathrm{x}_{2}\right)$ | $\mathrm{f}_{01}\left(\mathrm{x}_{1}, \mathbf{x}_{2}\right)$ | $\mathrm{f}_{10}\left(\mathrm{x}_{1}, \mathrm{x}_{2}\right)$ | $\mathrm{f}_{11}\left(\mathbf{x}_{1}, \mathbf{x}_{2}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 |

## Split the function into 4 functions

| $\mathbf{x}_{1}$ | $\mathbf{x}_{2}$ | $f_{00}\left(\mathbf{x}_{1}, x_{2}\right)$ | $\mathbf{f}_{01}\left(\mathbf{x}_{1}, x_{2}\right)$ | $\mathbf{f}_{10}\left(\mathbf{x}_{1}, \mathbf{x}_{2}\right)$ | $\mathbf{f}_{11}\left(\mathbf{x}_{1}, \mathbf{x}_{2}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 |

## Write Expressions for all four

| $\mathbf{x}_{1}$ | $\mathbf{x}_{2}$ | $\mathbf{f}_{00}\left(\mathbf{x}_{1}, \mathbf{x}_{2}\right)$ | $\mathbf{f}_{01}\left(\mathbf{x}_{1}, \mathbf{x}_{2}\right)$ | $\mathbf{f}_{10}\left(\mathbf{x}_{1}, \mathbf{x}_{2}\right)$ | $\mathbf{f}_{11}\left(\mathbf{x}_{1}, \mathbf{x}_{2}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 |

$\bar{x}_{1} \bar{x}_{2}$
$\bar{x}_{1} x_{2}$

## Then just add them together

| $\mathbf{x}_{1}$ | $\mathbf{x}_{2}$ | $\mathbf{f}_{00}\left(\mathbf{x}_{1}, \mathbf{x}_{2}\right)$ | $\mathrm{f}_{01}\left(\mathbf{x}_{1}, \mathbf{x}_{2}\right)$ | $\mathrm{f}_{10}\left(\mathbf{x}_{1}, \mathbf{x}_{2}\right)$ | $\mathrm{f}_{11}\left(\mathbf{x}_{1}, \mathbf{x}_{2}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 |

## $f\left(x_{1}, x_{2}\right)=\bar{x}_{1} \bar{x}_{2}+\bar{x}_{1} x_{2}+0+x_{1} x_{2}$

## Example 2.10

Implement the function $\mathrm{f}\left(\mathrm{x}_{1}, \mathrm{x}_{2}, \mathrm{x}_{3}\right)=\Sigma \mathrm{m}(2,3,4,6,7)$

## Minterms and Maxterms <br> (with three variables)

| Row <br> number | $x_{1}$ | $x_{2}$ | $x_{3}$ | Minterm | Maxterm |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | $m_{0}=\bar{x}_{1} \bar{x}_{2} \bar{x}_{3}$ | $M_{0}=x_{1}+x_{2}+x_{3}$ |
| 1 | 0 | 0 | 1 | $m_{1}=\bar{x}_{1} \bar{x}_{2} x_{3}$ | $M_{1}=x_{1}+x_{2}+\bar{x}_{3}$ |
| 2 | 0 | 1 | 0 | $m_{2}=\bar{x}_{1} x_{2} \bar{x}_{3}$ | $M_{2}=x_{1}+\bar{x}_{2}+x_{3}$ |
| 3 | 0 | 1 | 1 | $m_{3}=\bar{x}_{1} x_{2} x_{3}$ | $M_{3}=x_{1}+\bar{x}_{2}+\bar{x}_{3}$ |
| 4 | 1 | 0 | 0 | $m_{4}=x_{1} \bar{x}_{2} \bar{x}_{3}$ | $M_{4}=\bar{x}_{1}+x_{2}+x_{3}$ |
| 5 | 1 | 0 | 1 | $m_{5}=x_{1} \bar{x}_{2} x_{3}$ | $M_{5}=\bar{x}_{1}+x_{2}+\bar{x}_{3}$ |
| 6 | 1 | 1 | 0 | $m_{6}=x_{1} x_{2} \bar{x}_{3}$ | $M_{6}=\bar{x}_{1}+\bar{x}_{2}+x_{3}$ |
| 7 | 1 | 1 | 1 | $m_{7}=x_{1} x_{2} x_{3}$ | $M_{7}=\bar{x}_{1}+\bar{x}_{2}+\bar{x}_{3}$ |

## Minterms and Maxterms (with three variables)

| Row <br> number | $x_{1}$ | $x_{2}$ | $x_{3}$ | Minterm | Maxterm |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | $m_{0}=\bar{x}_{1} \bar{x}_{2} \bar{x}_{3}$ | $M_{0}=x_{1}+x_{2}+x_{3}$ |
| 1 | 0 | 0 | 1 | $m_{1}=\bar{x}_{1} \bar{x}_{2} x_{3}$ | $M_{1}=x_{1}+x_{2}+\bar{x}_{3}$ |
| 2 | 0 | 1 | 0 | $m_{2}=\bar{x}_{1} x_{2} \bar{x}_{3}$ | $M_{2}=x_{1}+\bar{x}_{2}+x_{3}$ |
| 3 | 0 | 1 | 1 | $m_{3}=\bar{x}_{1} x_{2} x_{3}$ | $M_{3}=x_{1}+\bar{x}_{2}+\bar{x}_{3}$ |
| 4 | 1 | 0 | 0 | $m_{4}=x_{1} \bar{x}_{2} \bar{x}_{3}$ | $M_{4}=\bar{x}_{1}+x_{2}+x_{3}$ |
| 5 | 1 | 0 | 1 | $m_{5}=x_{1} \bar{x}_{2} x_{3}$ | $M_{5}=\bar{x}_{1}+x_{2}+\bar{x}_{3}$ |
| 6 | 1 | 1 | 0 | $m_{6}=x_{1} x_{2} \bar{x}_{3}$ | $M_{6}=\bar{x}_{1}+\bar{x}_{2}+x_{3}$ |
| 7 | 1 | 1 | 1 | $m_{7}=x_{1} x_{2} x_{3}$ | $M_{7}=\bar{x}_{1}+\bar{x}_{2}+\bar{x}_{3}$ |

$$
f\left(x_{1}, x_{2}, x_{3}\right)=\sum m(2,3,4,6,7)
$$

- The SOP expression is:

$$
\begin{aligned}
f & =m_{2}+m_{3}+m_{4}+m_{6}+m_{7} \\
& =\bar{x}_{1} x_{2} \bar{x}_{3}+\bar{x}_{1} x_{2} x_{3}+x_{1} \bar{x}_{2} \bar{x}_{3}+x_{1} x_{2} \bar{x}_{3}+x_{1} x_{2} x_{3}
\end{aligned}
$$

- This could be simplified as follows:

$$
\begin{aligned}
f & =\bar{x}_{1} x_{2}\left(\bar{x}_{3}+x_{3}\right)+x_{1}\left(\bar{x}_{2}+x_{2}\right) \bar{x}_{3}+x_{1} x_{2}\left(\bar{x}_{3}+x_{3}\right) \\
& =\bar{x}_{1} x_{2}+x_{1} \bar{x}_{3}+x_{1} x_{2} \\
& =\left(\bar{x}_{1}+x_{1}\right) x_{2}+x_{1} \bar{x}_{3} \\
& =x_{2}+x_{1} \bar{x}_{3}
\end{aligned}
$$

## Example 2.12

Implement the function $\mathrm{f}\left(\mathrm{x}_{1}, \mathrm{x}_{2}, \mathrm{x}_{3}\right)=\Pi \mathrm{M}(0,1,5)$,
which is equivalent to $f\left(x_{1}, x_{2}, x_{3}\right)=\Sigma \mathrm{m}(2,3,4,6,7)$

## Minterms and Maxterms (with three variables)

| Row <br> number | $x_{1}$ | $x_{2}$ | $x_{3}$ | Minterm | Maxterm |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | $m_{0}=\bar{x}_{1} \bar{x}_{2} \bar{x}_{3}$ | $M_{0}=x_{1}+x_{2}+x_{3}$ |
| 1 | 0 | 0 | 1 | $m_{1}=\bar{x}_{1} \bar{x}_{2} x_{3}$ | $M_{1}=x_{1}+x_{2}+\bar{x}_{3}$ |
| 2 | 0 | 1 | 0 | $m_{2}=\bar{x}_{1} x_{2} \bar{x}_{3}$ | $M_{2}=x_{1}+\bar{x}_{2}+x_{3}$ |
| 3 | 0 | 1 | 1 | $m_{3}=\bar{x}_{1} x_{2} x_{3}$ | $M_{3}=x_{1}+\bar{x}_{2}+\bar{x}_{3}$ |
| 4 | 1 | 0 | 0 | $m_{4}=x_{1} \bar{x}_{2} \bar{x}_{3}$ | $M_{4}=\bar{x}_{1}+x_{2}+x_{3}$ |
| 5 | 1 | 0 | 1 | $m_{5}=x_{1} \bar{x}_{2} x_{3}$ | $M_{5}=\bar{x}_{1}+x_{2}+\bar{x}_{3}$ |
| 6 | 1 | 1 | 0 | $m_{6}=x_{1} x_{2} \bar{x}_{3}$ | $M_{6}=\bar{x}_{1}+\bar{x}_{2}+x_{3}$ |
| 7 | 1 | 1 | 1 | $m_{7}=x_{1} x_{2} x_{3}$ | $M_{7}=\bar{x}_{1}+\bar{x}_{2}+\bar{x}_{3}$ |

## $f\left(x_{1}, x_{2}, x_{3}\right)=\Pi M(0,1,5)$

- The POS expression is:

$$
\begin{aligned}
f & =M_{0} \cdot M_{1} \cdot M_{5} \\
& =\left(x_{1}+x_{2}+x_{3}\right)\left(x_{1}+x_{2}+\bar{x}_{3}\right)\left(\bar{x}_{1}+x_{2}+\bar{x}_{3}\right)
\end{aligned}
$$

- This could be simplified as follows:

$$
\begin{aligned}
f & =\left(x_{1}+x_{2}+x_{3}\right)\left(x_{1}+x_{2}+\bar{x}_{3}\right)\left(x_{1}+x_{2}+\bar{x}_{3}\right)\left(\bar{x}_{1}+x_{2}+\bar{x}_{3}\right) \\
& =\left(\left(x_{1}+x_{2}\right)+x_{3}\right)\left(\left(x_{1}+x_{2}\right)+\bar{x}_{3}\right)\left(x_{1}+\left(x_{2}+\bar{x}_{3}\right)\right)\left(\bar{x}_{1}+\left(x_{2}+\bar{x}_{3}\right)\right) \\
& =\left(\left(x_{1}+x_{2}\right)+x_{3} \bar{x}_{3}\right)\left(x_{1} \bar{x}_{1}+\left(x_{2}+\bar{x}_{3}\right)\right) \\
& =\left(x_{1}+x_{2}\right)\left(x_{2}+\bar{x}_{3}\right)
\end{aligned}
$$

## Two New Logic Gates

## NAND Gate



## NOR Gate



$$
\begin{array}{ll|l}
x_{1} & x_{2} & \mathrm{f} \\
\hline 0 & 0 & 1 \\
0 & 1 & 0 \\
1 & 0 & 0 \\
1 & 1 & 0
\end{array}
$$

## AND vs NAND



| $x_{1}$ | $x_{2}$ | f |
| :--- | :--- | :--- |
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |


| $x_{1}$ | $x_{2}$ | f |
| :--- | :--- | :--- |
| 0 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

## AND followed by NOT = NAND



| $x_{1}$ | $x_{2}$ | f |
| :--- | :--- | :--- |
| 0 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

## NAND followed by NOT = AND

| $x_{1}$ | $x_{2}$ | f |
| :--- | :--- | :--- |
| 0 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |


| f |
| :--- |
| 0 |
| 0 |
| 0 |
| 1 |



| $x_{1}$ | $x_{2}$ | f |
| :--- | :--- | :--- |
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

## OR vs NOR



$$
\begin{array}{ll|l}
x_{1} & x_{2} & \mathrm{f} \\
\hline 0 & 0 & 0 \\
0 & 1 & 1 \\
1 & 0 & 1 \\
1 & 1 & 1
\end{array}
$$

| $x_{1}$ | $x_{2}$ | f |
| :--- | :--- | :--- |
| 0 | 0 | 1 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 0 |

## OR followed by NOT = NOR



| $x_{1}$ | $x_{2}$ | f |
| :--- | :--- | :--- |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 1 |


| f |
| :--- |
| 1 |
| 0 |
| 0 |
| 0 |


| $x_{1}$ | $x_{2}$ | f |
| :--- | :--- | :--- |
| 0 | 0 | 1 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 0 |

## NOR followed by NOT = OR



| $x_{1}$ | $x_{2}$ | f |
| :--- | :--- | :--- |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 1 |

Why do we need two more gates?

## Why do we need two more gates?

They can be implemented with fewer transistors.
(more about this later)

## They are simpler to implement, but are they also useful?

## Building a NOT Gate with NAND



| $x$ | $\bar{x}$ |
| :---: | :---: |
| 0 | 1 |
| 1 | 0 |


| $x$ | $x$ | f |
| :--- | :--- | :--- |
| 0 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

## Building a NOT Gate with NAND



| $x$ | $\bar{x}$ |
| :---: | :---: |
| 0 | 1 |
| 1 | 0 |



## Building a NOT Gate with NAND



| $x$ | $\bar{x}$ |
| :---: | :---: |
| 0 | 1 |
| 1 | 0 |



Thus, the two truth tables are equal!

## Building an AND gate with NAND gates



Truth Table

| Input A | Input B | Output Q |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

## Building an OR gate with NAND gates



## Implications

## Any Boolean function can be implemented with only NAND gates!

## NOR gate with NAND gates

Desired NOR Gate
NAND Construction


= NOT\{ NOT[ NOT( A AND A ) AND
NOT( B AND B )]\}

| Truth Table |  |  |
| :---: | :---: | :---: |
| Input A | Input B | Output Q |
| 0 | 0 | 1 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 0 |

## XOR gate with NAND gates

Desired XOR Gate

$\mathbf{Q}=\mathbf{A} \operatorname{XOR} \mathbf{B}$

NAND Construction

$=$ NOT[ NOT\{A AND NOT(A AND B) $\}$ AND
NOT\{B AND NOT(A AND B)\}]
Truth Table

| Input A | Input B | Output Q |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

## XNOR gate with NAND gates

Desired XNOR Gate
NAND Construction


$\mathbf{Q}=\operatorname{NOT}(\mathbf{A X O R B})$

| Truth Table |  |  |
| :---: | :---: | :---: |
| Input A Input B Output Q |  |  |
| 0 | 0 | 1 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

## Building a NOT Gate with NOR



| $x$ | $\bar{x}$ |
| :---: | :---: |
| 0 | 1 |
| 1 | 0 |


| $x$ | $x$ | f |
| :--- | :--- | :--- |
| 0 | 0 | 1 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 0 |

## Building a NOT Gate with NOR



| $x$ | $\bar{x}$ |
| :---: | :---: |
| 0 | 1 |
| 1 | 0 |



## Building a NOT Gate with NOR



Thus, the two truth tables are equal!

## Building an OR gate with NOR gates

Desired Gate
NOR Construction



| Truth Table |  |  |
| :---: | :---: | :---: |
| Input A | Input B | Output Q |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 1 |

## Let's build an AND gate with NOR gates

## Let's build an AND gate with NOR gates



NOR Construction


Truth Table

| Input A | Input B | Output Q |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

## Implications

## Any Boolean function can be implemented with only NOR gates!

## NAND gate with NOR gates



## XOR gate with NOR gates



Truth Table

| Input A | Input B | Output Q |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

## XNOR gate with NOR gates

Desired XNOR Gate
NOR Construction



Truth Table

| Input A | Input B | Output Q |
| :---: | :---: | :---: |
| 0 | 0 | 1 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

The following examples came from this book


[ Platt 2009]

[ Platt 2009]

[ Platt 2009 ]

[ Platt 2009]

[ Platt 2009]

[Platt 2009 ]

## DeMorgan's theorem in terms of logic gates



## DeMorgan's theorem in terms of logic gates



## Function Synthesis

## Using NAND gates to implement a sum-of-products


[ Figure 2.27 from the textbook]

## Using NOR gates to implement a product-of sums


[ Figure 2.28 from the textbook ]

## Example 2.13

Implement the function $f\left(x_{1}, x_{2}, x_{3}\right)=\Sigma \mathrm{m}(2,3,4,6,7)$ using only NOR gates.

## Example 2.13

Implement the function $\mathrm{f}\left(\mathrm{x}_{1}, \mathrm{x}_{2}, \mathrm{x}_{3}\right)=\Sigma \mathrm{m}(2,3,4,6,7)$ using only NOR gates.

The POS expression is: $f=\left(x_{1}+x_{2}\right)\left(x_{2}+\bar{x}_{3}\right)$

## NOR-gate realization of the function


(a) POS implementation

(b) NOR implementation

## Example 2.14

Implement the function $\mathrm{f}\left(\mathrm{x}_{1}, \mathrm{x}_{2}, \mathrm{x}_{3}\right)=\Sigma \mathrm{m}(2,3,4,6,7)$ using only NAND gates.

## Example 2.14

Implement the function $\mathrm{f}\left(\mathrm{x}_{1}, \mathrm{x}_{2}, \mathrm{x}_{3}\right)=\Sigma \mathrm{m}(2,3,4,6,7)$ using only NAND gates.

The SOP expression is: $f=x_{2}+x_{1} \bar{x}_{3}$

## NAND-gate realization of the function


(a) SOP implementation

(b) NAND implementation
[ Figure 2.30 from the textbook ]

## Questions?

## THE END

