## CprE 281: Digital Logic

Midterm 1: Friday Sep 22, 2017
Student Name: $\qquad$

## Student ID Number:

$\qquad$

| Lab Section: | Mon 9-12(N) | Tue 11-2(U) | Wed 8-11(J) | Thur 11-2(Q) | Fri 11-2(G) |
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| (circle one) | Mon 12-3(P) | Tue 2-5(M) | Wed 11-2(W) | Thur 11-2(V) |  |
|  |  | Tue 2-5(Z) | Wed 6-9(T) | Thur 2-5(L) |  |
|  |  |  |  | Thur 5-8(K) |  |

1. $\quad$ True/False Questions ( $10 \times 1 \mathrm{p}$ each $=10 \mathrm{p}$ )
(a) I forgot to write down my name, student ID, and lab section.

TRUE / FALSE
(b) A 2-to-1 multiplexer can be built using only OR and NOT gates.
(c) It is not possible to build a NOT gate with a 2-to-1 multiplexer.

TRUE / FALSE
(d) The minimum expression for $\mathrm{f}(\mathrm{x}, \mathrm{y})=\sum \mathrm{m}(0,1,3)+\mathrm{D}(2)$ is 1 . TRUE / FALSE
(e) $\overline{\mathrm{a} \cdot \mathrm{c}}+\mathrm{a} \cdot \mathrm{c}=1$

TRUE / FALSE
(f) $\overline{\bar{x} y}=x \bar{y}$
(g) $\mathrm{m}_{0}+\mathrm{m}_{1}=\overline{\mathrm{M}_{0} \cdot \mathrm{M}_{1}}$
(h) $\overline{\mathrm{x} \cdot \mathrm{y}}=\overline{\mathrm{x}}+\overline{\mathrm{x}}$
(i) The ' K ' in K-map stands for 'Kilobyte.'

TRUE / FALSE
(j) K-2SO is stronger than C-3PO.

TRUE / FALSE

## 2. Three-Variable K-map (5p)

Draw the K-map and derive the minimum $\underline{\mathbf{S O P}}$ expression for $\mathbf{f}(\mathbf{a}, \mathbf{b}, \mathbf{c})=\Pi \mathbf{M}(\mathbf{2}, \mathbf{4}, \mathbf{5})$.
3. Minimization ( $3 \times 5 p$ each $=15 p$ )
(a) Draw the truth table for the Boolean function $f(x, y, z)=x \bar{z}+\bar{x}(z+\bar{y})$
(b) Draw the K-map for this function and derive the minimum cost $\underline{\text { POS }}$ expression.
(c) Draw the circuit diagram for the minimum cost POS expression.
4. Number Conversions ( $5 \times 4 p$ each $=20 p$ )
(a) Convert $243_{5}$ to decimal
(b) Convert $193_{10}$ to binary
(c) Convert $\mathrm{DC}^{2} \mathrm{~B}_{16}$ to binary
(d) Find the value of the base $\mathbf{x}$ in the following equation: $12_{x}=1011_{2}$
(e) Compute the following sum and write the answer in octal:
$1101001_{2}+81_{16}=?_{8}$
5. Verilog to Circuit ( $2 \times 5 p$ each $=10 p$ )
(a) Draw the circuit diagram that corresponds to the Verilog module shown below. Label all inputs and outputs.
module mystery (A, B, C, D, F);
input $A, B, C, D ;$
output F;
$\operatorname{assign} F=(A \& B)|(\sim B \& C)| D ;$ endmodule
(b) Redraw the circuit from (a) using only NAND gates.
6. Circuit to Circuit Conversion ( $3 \times 5$ peach $=15 p$ )
(a) Write the expression for the function F given by this circuit (don't simplify it yet).

(b) Use the theorems of Boolean algebra to simplify the expression from part (a).
(c) Draw the circuit for your expression from part (b). Label all inputs and outputs.
7. Derive the minimum SOP expression using a K-map ( $3 \times 5 \mathrm{p}$ each $=15 \mathrm{p}$ )
(a) Draw the K-map for the following function

$$
\mathrm{F}(\mathrm{a}, \mathrm{~b}, \mathrm{c}, \mathrm{~d})=\Sigma \mathrm{m}(1,3,8,9,10,12,14,15)+\mathrm{D}(2,4,5,11)
$$

(b) Use the K-map to derive the minimum-cost SOP expression for the function $F$.
(c) Draw the circuit diagram for the minimum expression from part (b).
8. NAND/NOR Logic ( $2 \times 5$ peach $=10 p$ )
(a) Using only NAND gates, draw the logic circuit that corresponds to the truth table shown below. Hint: Start by writing and then modifying the expression for $F$.

| $\mathbf{X}$ | $\mathbf{Y}$ | $\mathbf{F}$ |
| :--- | :--- | :--- |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ |
| $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ |
| $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{0}$ |
| $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ |

(b) Draw the circuit that corresponds to the following K-map using only NOR gates.

| A B |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| C | 00 | 01 | 11 | 10 |
| 0 | 1 | 1 | 1 | 0 |
| 1 | d | 1 | 0 | 0 |

9. Joint Optimization ( $3 \times 5$ peach $=15 p$ )

The outputs $f$ and $g$ of a two-output circuit are specified with the following expressions:
$\mathrm{f}(\mathrm{a}, \mathrm{b}, \mathrm{c}, \mathrm{d})=\boldsymbol{\operatorname { m }}(1,4,5,8,15)+\mathrm{D}(0,2,6,9)$
$\mathrm{g}(\mathrm{a}, \mathrm{b}, \mathrm{c}, \mathrm{d})=\Sigma \mathrm{m}(0,4,5,10,15)+\mathrm{D}(2,8,9,11)$
(a) Draw the K-map for $f$
and
the K-map for g
(b) Derive the jointly optimized SOP expressions for $f$ and $g$ such that the two expressions share two implicants. Note that these are not necessarily prime implicants.
(c) Draw the diagram for the jointly optimized circuit. Indicate which logic gates are shared by drawing arrows that point to them. Label all inputs and outputs.

## 10. Minimization with Theorems (15p)

Use the theorems of Boolean algebra to simplify the following Boolean function

$$
f(w, x, y, z)=y(\bar{y}+z)+(\bar{y}+w \bar{y}(x z+x \bar{z})) z+(\overline{x \bar{y}}+\overline{(x+y)}+\bar{z})+y(z+w \bar{x}(\bar{w}+z))
$$

| Question | Max | Score |
| :--- | ---: | :--- |
| 1. True/False | 10 |  |
| 2. Three-variable K-map | 5 |  |
| 3. Minimization | 15 |  |
| 4. Number Conversions | 20 |  |
| 5. Verilog to Circuit | 10 |  |
| 6. Circuit to Circuit | 15 |  |
| 7. SOP with K-Map | 15 |  |
| 8. NAND/NOR Logic | 10 |  |
| 9. Joint Optimization | 15 |  |
| 10. Minimization | 15 |  |
| TOTAL: | 130 |  |

