

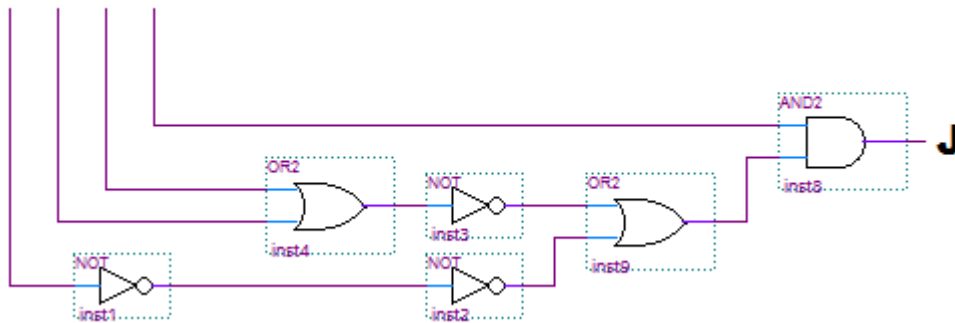
P1 (5 points): A given circuit takes V , a 7-bit binary number, divides V by 5, and stores the quotient and remainder into Q and R , respectively. (e.g. if $V=13$, then $Q=2$ and $R=3$).

A: How many bits are needed to represent all possible values of Q .

B: How many bits are needed to represent R .

P2 (5 points): For the circuit below, show the combinations of inputs that will yield the output $J=1$.

W X Y Z



P3 (10 points): Using a Venn diagram, show that $\overline{xy} \neq \overline{(xy)}$

P4 (10 points): Draw the circuit for the following expressions:

$$X = \overline{a}b + \overline{(cd)}$$

$$Y = a + b + \overline{(a + bc)} + abc$$

P5 (20 points): Given the following expression $G = (A\overline{B} + C\overline{D})(\overline{A}C + B\overline{D})$:

A. Let the circuit cost be defined as the number of gates plus the number of gate inputs. Draw the circuit for G , then show that the cost of this circuit is 27. You may have to reuse a gate to reduce the cost; the circuit should be drawn appropriately to reflect the cost.

B. Use Boolean algebra to simplify the expression for G .

C. Draw the circuit for G and state the new cost of the circuit.

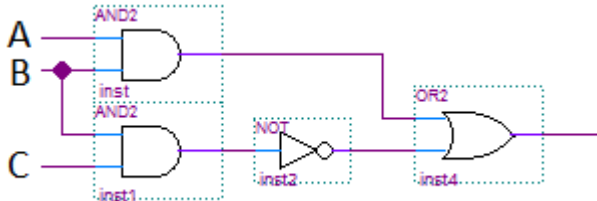
P6 (10 points): Use Boolean Algebra to simplify the following expressions:

A: $wx\overline{y}z + wx\overline{y}\overline{z} + wxy\overline{z} + wxyz + w\overline{x}y\overline{z}$

B: $(\overline{p} + \overline{q} + r)(\overline{q} + r + \overline{s})(\overline{p} + q + r)(\overline{q} + \overline{r} + \overline{s})$

C: $w + wx\overline{y} + wx\overline{z} + w\overline{x}y + w\overline{x}z$

P7 (10 points): For the circuit below,
A: show the truth table for the circuit and
B: prove that the output of the circuit matches the expression that follows:



$$= a + b' + c'$$

P8 (10 points): Given the following truth table for F, write the expression for F in canonical sum-of-products notation and in canonical product-of-sums notation.

L	M	N	F
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

P9 (10 points): Use DeMorgan's Theorem to determine the complement of each expression:

$$A = wx + w\bar{y} + \bar{w}z + \bar{x}\bar{y} + \bar{x}\bar{z} + \bar{y}\bar{z}$$

$$B = p + \bar{q}(\bar{r} + s\bar{v})$$

P10 (10 points): Use Boolean Algebra to prove the following expressions as equivalent:

I: $(a + b)\overline{(a + c)} + \overline{(a + b + c)} = \overline{a + c}$

II: $w\bar{x} + wxy + \bar{w} + \bar{w}(xy) = \bar{w} + \bar{x} + y$

III: $\overline{(pr + \bar{p}r)} + \bar{q}(\bar{p}r + pr) + qr = 1$