

P1. (20 points) Use a K-map to find the minimal sum-of-products (SOP) expression for the following four problems. Show the terms that are grouped in each K-map.

a) (5 points)

		BC			
		00	01	11	10
A	0	0	0	0	1
	1	1	0	0	1

b) (5 points)

		CD			
		00	01	11	10
AB	00	1	0	0	1
	01	0	1	1	0
	11	0	0	0	0
	10	1	0	0	1

c) (5 points) $F(A, B, C) = \sum m(1, 2, 3, 5, 7)$

d) (5 points) $F(A, B, C, D) = \sum m(1, 3, 4, 5, 6, 7, 9, 11, 13, 15)$

P2. (15 points) Use a K-map to find the minimal product-of-sums (POS) expression for the following three problems. Show the terms that are grouped in each K-map.

a) (5 points)

		BC			
		00	01	11	10
A	0	0	0	0	1
	1	1	0	0	1

b) (5 points)

		CD			
		00	01	11	10
AB	00	1	0	0	1
	01	0	1	1	0
	11	0	1	1	0
	10	1	0	0	1

c) (5 points) $F(A, B, C, D) = \prod M(5, 7, 11, 13, 15)$

P3. (4x5=20 points) You stumble across an old manuscript containing the following page, but some ink stains are obscuring part of the content. Deduce the function $F(A,B,C)$ and write: a) the complete K-map; b) the complete truth table; c) the minimized POS expression; and d) the minimized SOP circuit diagram. Explain your reasoning.

A	B	C	F
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	1

(1) Truth Table

$$F(A,B,C) = (A + \bar{B} + C)$$

(2) Minimized POS Expression

(3) Minimized SOP circuit

Representations of function $F(A,B,C)$

P4. (10 points) Use a K-map to derive the minimal SOP expressions for the following Boolean function:

$$F(A,B,C,D) = ACD' + C'D + AB' + ABCD$$

P5. (15 points) Design a circuit that accepts a 4-bit number $X = x_3x_2x_1x_0$ as input and generates a 1-bit output P that is equal to 1 if the input number is a prime. (0 and 1 are not prime; 2, 3, 5, etc., are prime.)

- (7 points) Write down the truth table for the output P .
- (8 points) Derive the simplest SOP expressions for the output P .

P6. (20 points) Design a circuit that accepts a 3-bit number $X = x_2x_1x_0$ as input and generates a 6-bit number $Y = y_5y_4y_3y_2y_1y_0$ as output, which is equal to the square of the input number (i.e., $Y = X^2$).

- (10 points) Write down the truth table for the six output lines $y_5y_4y_3y_2y_1y_0$ that jointly represent the number Y in binary.
- (10 points) Derive the simplest SOP expressions for each bit of the output. That is, derive six expressions: one for y_5 , another for y_4 , and so on.